

# Towards Incremental Language Definition with Reusable Components

Damian Frölich and Thomas van Binsbergen

Informatics Institute, University of Amsterdam  
[{dfrolich,ltvanbinsbergen}@acm.org](mailto:{dfrolich,ltvanbinsbergen}@acm.org)

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## Incremental programming

- Stepwise
- Submitting small snippets of code
- Immediate feedback

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The screenshot shows a Jupyter notebook interface with the title "jupyter 1\_tutorial\_voting [unsaved changes]" at the top. The notebook contains a section titled "eFLINT Tutorial - Voting" which includes a copyright notice and a disclaimer about the purpose of the document. Below this, there is a heading "Fact-type declarations" followed by a note about the nature of fact-type declarations. Two code cells are shown:

In [1]:

```
Fact citizen  
Fact candidate  
Fact administrator
```

Depending on where they occur, identifiers such as `citizen`, `candidate`, and `administrator` can play different roles. For example, when occurring in an expression, an identifier is a placeholder for an instance of the type with the same name. Identifiers can also be used to refer to types themselves and to constructors for creating instances of types, as is shown later.

In the previous fragment, the declared types are all atomic with instances coming from the set of (all) strings. To make this explicit, the following type declarations could have been used instead (i.e. are equivalent), indicating that the instances of the types are identified by string literals:

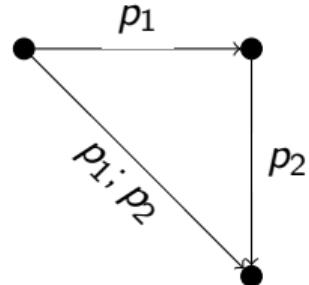
In [2]:

```
Fact citizen IdentifiedBy String  
Fact candidate IdentifiedBy String  
Fact administrator IdentifiedBy String
```

The following code fragments are examples of expressions referring to instances of a fact-type: `citizen("Alice")`, `candidate("John")`, and `administrator("abc1234")`. String literals are arbitrary sequences of characters between double quotes, or are a sequence of alphanumeric characters starting with a capital alphabetical. As such, "`Alice`" and `Alice` are referring to the same string literal. Besides string literals, also integer literals are available (`IdentifiedBy Int`).

The instances of a fact-type, facts, can be considered as variables to which a truth-value can be assigned. As such, a fact can be considered to hold true, hold false or be undetermined in a given situation. The following statement makes the instance `citizen("Alice")` hold true:

# Sequential languages<sup>1</sup>



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<sup>1</sup>A principled approach to REPL interpreters. Van Binsbergen, et al.

## Incremental language development

Compose languages without losing flexibility while promoting reusability

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- Compose language constructs
- Compose language construct semantics

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- Compose language constructs
- Compose language construct semantics
  - ⇒ the Expression Problem
  - .∴ Data types 'a la carte (DTC)
- Promote re-use and compatibility
  - .∴ Use funcons as a lingua franca

# Incremental language development

Compose languages without losing flexibility while promoting reusability

- Compose language constructs
- Compose language construct semantics
  - ⇒ the Expression Problem
  - ∴ Data types 'a la carte (DTC)
- Promote re-use and compatibility
  - ∴ Use funcons as a lingua franca
- Modify the structure of the language
  - ∴ A new approach for language definitions

## Data types 'a la carte<sup>2</sup>

```
data Num a = Num int
    deriving Functor
data Add a = Add a a
    deriving Functor
data Lang = Fix (Num :+: Add)
data Fix f = In (f (Fix f))
```

---

<sup>2</sup>Swierstra, JFP 2008

## Data types 'a la carte<sup>2</sup>

```
data Num a = Num int
    deriving Functor
data Add a = Add a a
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data Lang = Fix (Num :+: Add)
data Fix f = In (f (Fix f))
```

```
foldLang :: Functor f -> (f a -> a)
          -> Fix f -> a
instance Eval Num where
    eval (Num n) = n
instance Eval Add where
    eval (Add e1 e2) = e1 + e2
```

---

<sup>2</sup>Swierstra, JFP 2008

## Funcons<sup>4</sup>

- Component-based approach towards formal, dynamic semantics
- A library of reusable, fundamental constructs (funcons)
- Executable micro-interpreters<sup>3</sup>

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<sup>3</sup>Executable Component-Based Semantics. Van Binsbergen, Sculthorpe, Mosses. JLAMP 2019

<sup>4</sup>PLanCompS project lead by Peter Mosses

## Funcons<sup>4</sup>

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**apply(bound("f"), integer-add(12))**

---

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## Contribution

A method that supports incremental language definition via composition by delaying language structure choices

## Language structure

$$Var_{\emptyset} : String \rightarrow Expr$$
$$Abs_{\emptyset} : String \times Expr \rightarrow Expr$$
$$App_{\emptyset} : Expr \times Expr \rightarrow Expr$$

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Language structure is decided by the types of our constructors

# Delayed language structure

## Operator declarations

introduces operators, arities and name 'operand positions'

$\text{Var}_{\mathcal{O}} : \text{VarVar}$

$\text{Abs}_{\mathcal{O}} : \text{AbsVar} \times \text{AbsBody}$

$\text{App}_{\mathcal{O}} : \text{AppAbs} \times \text{AppArg}$

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## Sort constraints

assign (one or more) operators to (possibly new) sorts.

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assign (one or more) operators to (possibly new) sorts.

## Operator assignments

$$\text{Var}_{\mathcal{O}} \in \text{AbsBody}$$

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## Sort constraints

assign (one or more) operators to (possibly new) sorts.

## Operator assignments

$$Var_{\mathcal{O}} \in AbsBody$$
$$Var_{\mathcal{O}} \in Expr$$
$$App_{\mathcal{O}} \in Expr$$
$$Abs_{\mathcal{O}} \in Expr$$

# Delayed language structure

## Operator declarations

introduces operators, arities and name 'operand positions'

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## Sort constraints

assign (one or more) operators to (possibly new) sorts.

## Operator assignments

$$Var_{\mathcal{O}} \in AbsBody$$

$$Var_{\mathcal{O}} \in Expr$$

$$App_{\mathcal{O}} \in Expr$$

$$Abs_{\mathcal{O}} \in Expr$$

## Sub-sort constraints

$$Expr \subseteq AbsBody$$

$$Expr \subseteq AppAbs$$

$$Expr \subseteq AppArg$$

# Operator semantics

$Var_{\mathcal{F}}(lit) = \text{bound string } lit$

$Abs_{\mathcal{F}}(x, b) = \text{function closure scope}(\text{bind(string } x, \text{given}), b)$

$App_{\mathcal{F}}(abs, arg) = \text{apply}(abs, arg)$

Semantic functions translate operator occurrences to funcon terms (semantic domain).

# Operator semantics

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Semantic functions translate operator occurrences to funcon terms (semantic domain).

Existing operator semantics not always enough for every language

# Operator specialization

Associating ‘wrapper funcon terms’ as part of sort constraints

$Return_{\emptyset} : ReturnVal$  (Operator declaration)

$Return_{\mathcal{F}}(val) = \mathbf{return} val$  (Semantic function)

$Return_{\emptyset} \in AbsBody$  (Sort constraint with glue code)

$\hookrightarrow \mathbf{handle-return}(AbsBody_{\mathcal{F}})$  (glue code)

# Language definition

## Definition

A language  $L$  is a structure  $\langle O, T, S, F, G, I \rangle$  with:

- $O$  a set of operators,
- $T \subset O$  the set of operators assigned to the top-level,
- $S$  a family of sets representing operator assignments
- $F$  a family of functions representing the semantic functions
- $G$  a family of glue functions
- $I$  a function for initialisation over top-level operators

# Implementation

```
data Abs u t where
    Abs :: IsTrue (AbsBody t) => String -> u t -> Abs u AbsType
data AbsType
type family AbsBody t
```

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    Abs :: IsTrue (AbsBody t) => String -> u t -> Abs u AbsType
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type family AbsBody t
$(genSortConstraint [(''AbsType, ''AbsBody)])
 $\implies \text{Abs}_{\emptyset} \in \text{AbsBody}$ 
```

# Implementation

```
data Abs u t where
    Abs :: IsTrue (AbsBody t) => String -> u t -> Abs u AbsType
data AbsType
type family AbsBody t
$(genSortConstraint [(''AbsType, ''AbsBody)])
 $\implies \text{Abs}_{\emptyset} \in \text{AbsBody}$ 
type family Expr t
$(genSortConstraint [(''AbsType, ''Expr)])
$(genSubSort [(''Expr, ''AbsBody)])
 $\implies \text{Abs}_{\emptyset} \in \text{Expr}$ 
 $\text{Expr} \subseteq \text{AbsBody}$ 
```

## Semantics

```
instance ToFuncons Abs where
    toFuncons (Abs s (K body)) = K $
        function [closure [scope [bind [string s, given], body]]]
```

## Glue code

```
$(genGlue (''AbsBody, ''P(Command), ''absGlueReturn))  
absGlueReturn command_f = handle_return [command_f]
```

## Glue code

```
$ (genGlue (''AbsBody, ''P(Command), ''absGlueReturn))  
absGlueReturn command_f = handle_return [command_f]  
 $\implies$   
instance GetGlue AbsGlue Command Funcons where  
    getGlue AbsVarGlue _ = id  
    getGlue AbsBodyGlue l = absGlueReturn  
  
class GetGlue operand (f :: (* -> *) -> * -> *) target where  
    getGlue :: operand -> f (Term a) b -> target -> target  
    getGlue _ _ = id
```

## Why we delay

```
data Language = Language
{ operators :: [Operator]
, op_assign :: [OperatorAssignment]
, sub_sorts :: [SubSort]
, glue_code :: [(Sort, MetaType, GlueFunction)]
, init_code :: [(MetaType, GlueFunction)]}
} deriving (Show)
```

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} deriving (Show)
```

```
type family Expr
lambdaLanguage = Language
operators =
  [(Var, VarType), (Abs, AbsType),
   (App, AppType)]
op_assign =
  [(op, Expr) | op <-
    [VarType, AbsType, AppType]]
sub_sorts =
  [(Expr, t) | t <-
    [AbsBody, AppLeft, AppRight, TopLevel]],
  ...
})
```

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{ operators :: [Operator]
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<*> :: Language -> Language -> Language
```

```
type family Expr
lambdaLanguage = Language
operators =
[(''Var, ''VarType), (''Abs, ''AbsType),
 (''App, ''AppType)]
,op_assign =
[(op, ''Expr) | op <-
 [''VarType, ''AbsType, ''AppType]]
,sub_sorts =
[(''Expr, t) | t <-
 [''AbsBody, ''AppLeft, ''AppRight, ''TopLevel]],
 ...
})
```

## Example

```
import Lambda(Expr)
arithLanguage = Language
{ operators = [(''Add, ''AddType), (''IntV, ''IntVType)]
, op_assign = [(op, ''Expr) | op <- [''AddType, ''IntVType]]
, sub_sorts = [(''Expr, t) | t <- [''AddLeft, ''AddRight]]
...
}
```

Can now extend the lambda language with the arithmetic language (extension)

```
lambdaLanguage <*> arithLanguage
```

## Example

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import Lambda(Expr)
arithLanguage = Language
{ operators = [(''Add, ''AddType), (''IntV, ''IntVType)]
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Without a dependency (unification)

```
lambdaLanguage <*> arithLanguage <*> arithLambdaGlue
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lambdaLanguage <*> arithLanguage
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Without a dependency (unification)

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lambdaLanguage <*> arithLanguage <*> arithLambdaGlue
```

With restriction

```
functional = lambdaLanguage <*> arithLanguage <*> modExceptionsLanguage
where
    modExceptionsLanguage = exceptionsLanguage {
        op_assign = removeCatch $ op_assign modExceptionsLanguage
        sub_sorts = removeCatch $ sub_sorts modExceptionsLanguage }
```

## Example

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import Lambda(Expr)
arithLanguage = Language
{ operators = [(''Add, ''AddType), (''IntV, ''IntVType)]
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    modExceptionsLanguage = exceptionsLanguage {
        op_assign = removeCatch $ op_assign modExceptionsLanguage
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```

Correspond to the operations used by Erdweg

# Conclusion

## Approach

- + Highly flexible
- + Permits rapid prototyping
- Difficult to track composition effects

## Implementation

- + Properties are statically checked by Haskell
- + Languages are just Haskell data types
- + Semantic functions are just Haskell functions
- Interactivity hampered by Template Haskell
- Language definitions can be verbose

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## Future work

- Development of an external DSL to fully utilise interactivity
- User defined concrete syntax
- Explore other algebras

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